

Invasion

Evolution and Ecology

- Population Genetics
- Game Theory
- Life History Theory
- Community Ecology

Population Genetics

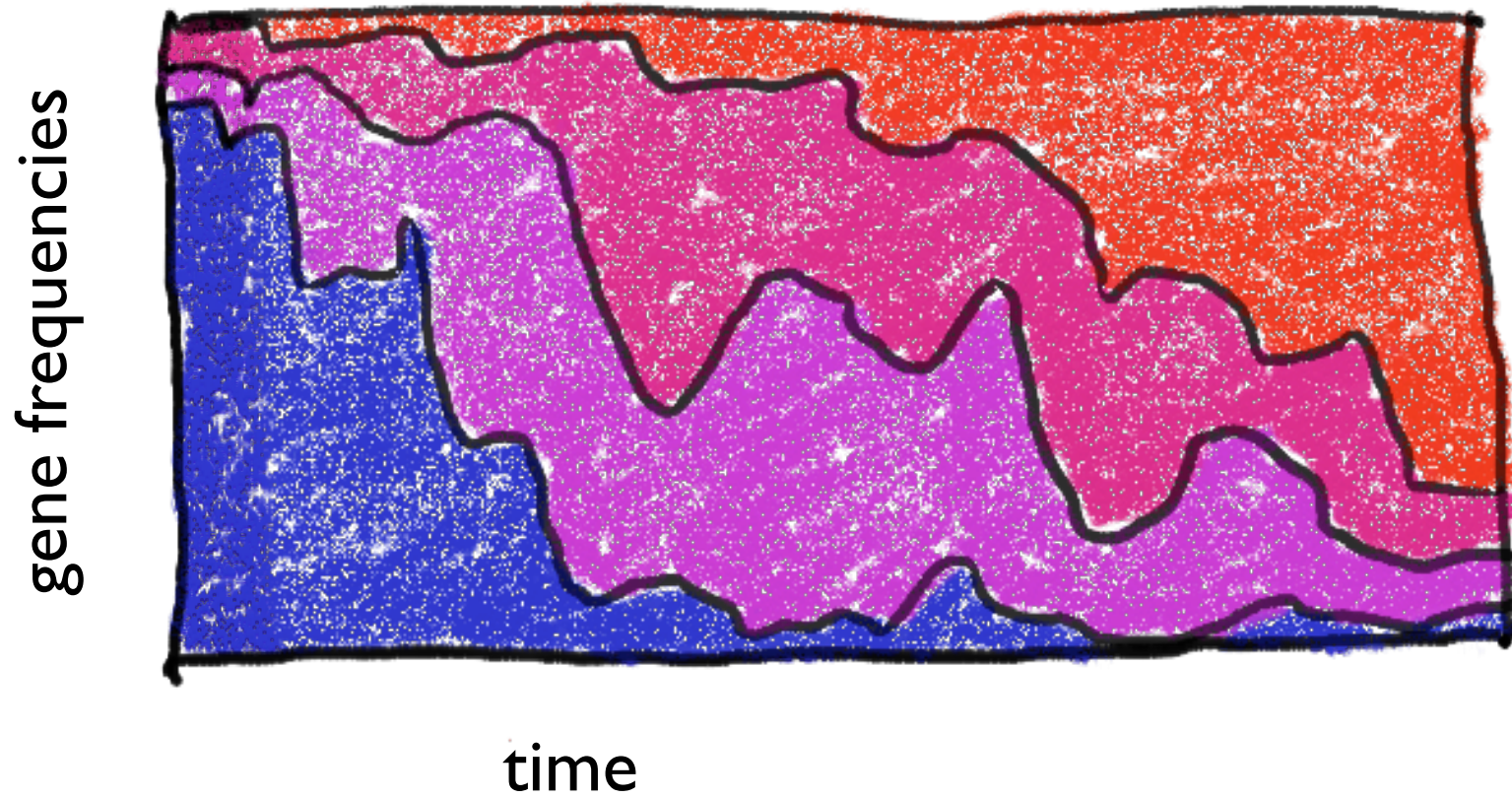
Population Genetics

Well-known standard case:

- Sexual reproduction
- Diploid genetics
- Two alleles (dominant/recessive)

Variables: **gene frequencies**

Gene frequencies



Population Genetics

Typical assumptions:

- single population
- simplified ecology
 - most ecological aspects are subsumed in ‘frequency dependence’
- more realistic cases difficult to analyse
 - density dependence
 - population interactions

$$\frac{dx_i}{dt} = (b_i - d_i) x_i$$
$$= r_i x_i$$

$$i = a, A$$

may be
density dependent!
 $r_i = f_i(\dots, x_j, \dots)$

$$p_a = \frac{x_a}{x_a + x_A}$$

$$\frac{dp_a}{dt} = \frac{\frac{dx_a}{dt}(\cancel{x_a + x_A}) - x_a(\cancel{\frac{dx_a}{dt}} + \frac{dx_A}{dt})}{(x_a + x_A)^2}$$

$$= \frac{\frac{dx_a}{dt} x_A - x_a \frac{dx_A}{dt}}{(x_a + x_A)^2}$$

$$= \frac{r_a x_a x_A - r_A x_A x_a}{(x_a + x_A)^2}$$

$$= \frac{x_a x_A}{(x_a + x_A)^2} (r_a - r_A)$$

$$= p_a (1 - p_a) (r_a - r_A)$$

If $r_a = r_A (1 + s)$

then $\frac{dp_a}{dt} = p_a (1 - p_a) r_A s$

"Selection coefficient"

Measures of increase

Subtle differences

- λ rate of population increase
 - invasion continuous time : $\lambda > 0$
 - invasion discrete time : $\lambda > 1$
- R_0 basic reproduction ratio of individuals
 - invasion : $R_0 > 1$
- r net rate of reproduction of population
 - invasion : $r > 0$
- s selection coefficient
 - increase in frequency : $s > 0$

Population Genetics

Much attention to

- interaction among alleles and loci
 - dominance
 - modifiers
 - conditions that favour **polymorphism**
 - epistasis, linkage
 - links with developmental biology

Population Genetics

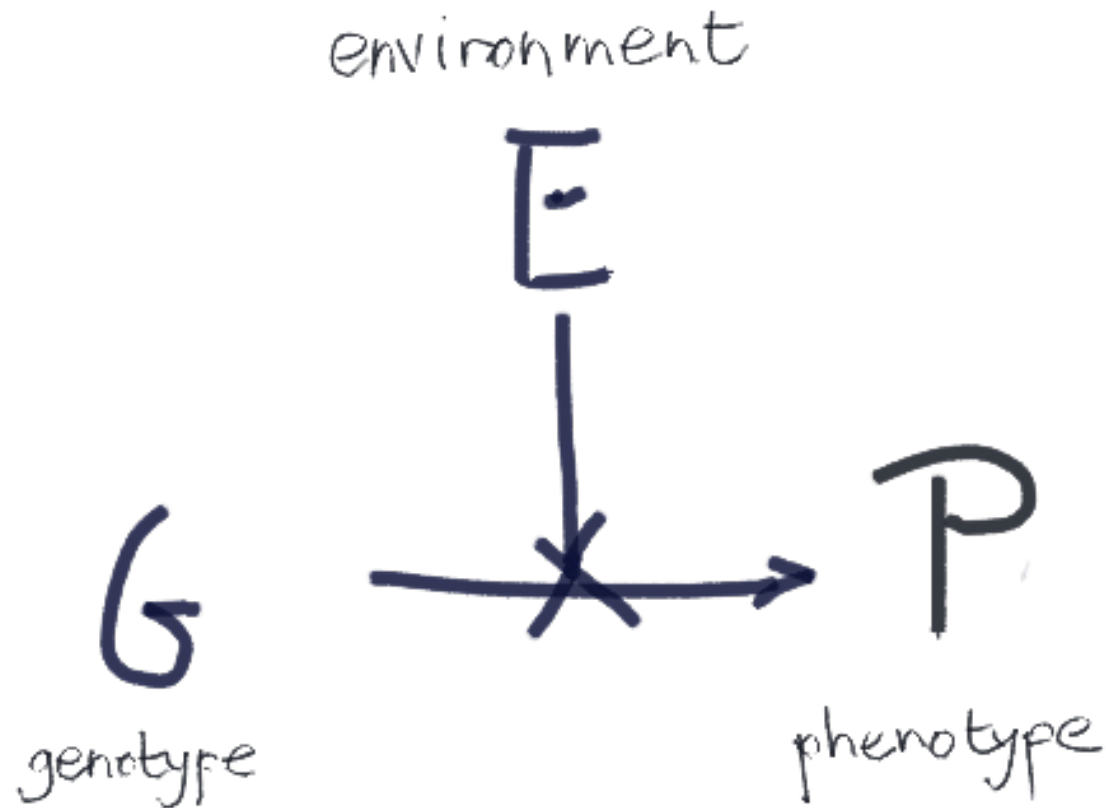
Little attention to

- Interactions among individuals

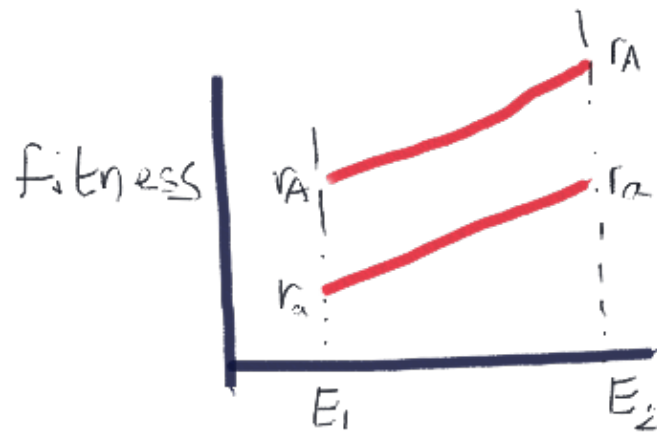
- Population dynamics and ecology
- Behaviour

density dependence
phenotypic plasticity

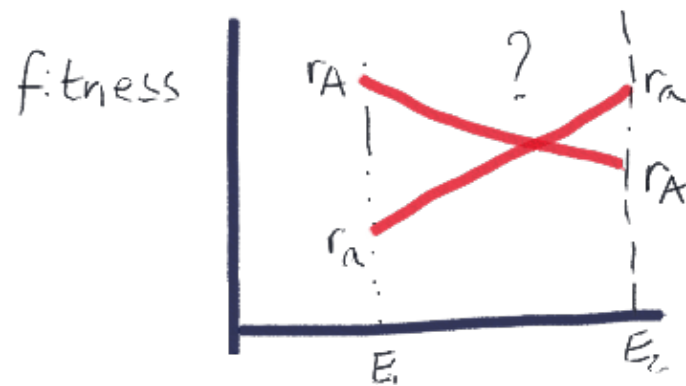
Phenotypic plasticity



Phenotypic plasticity

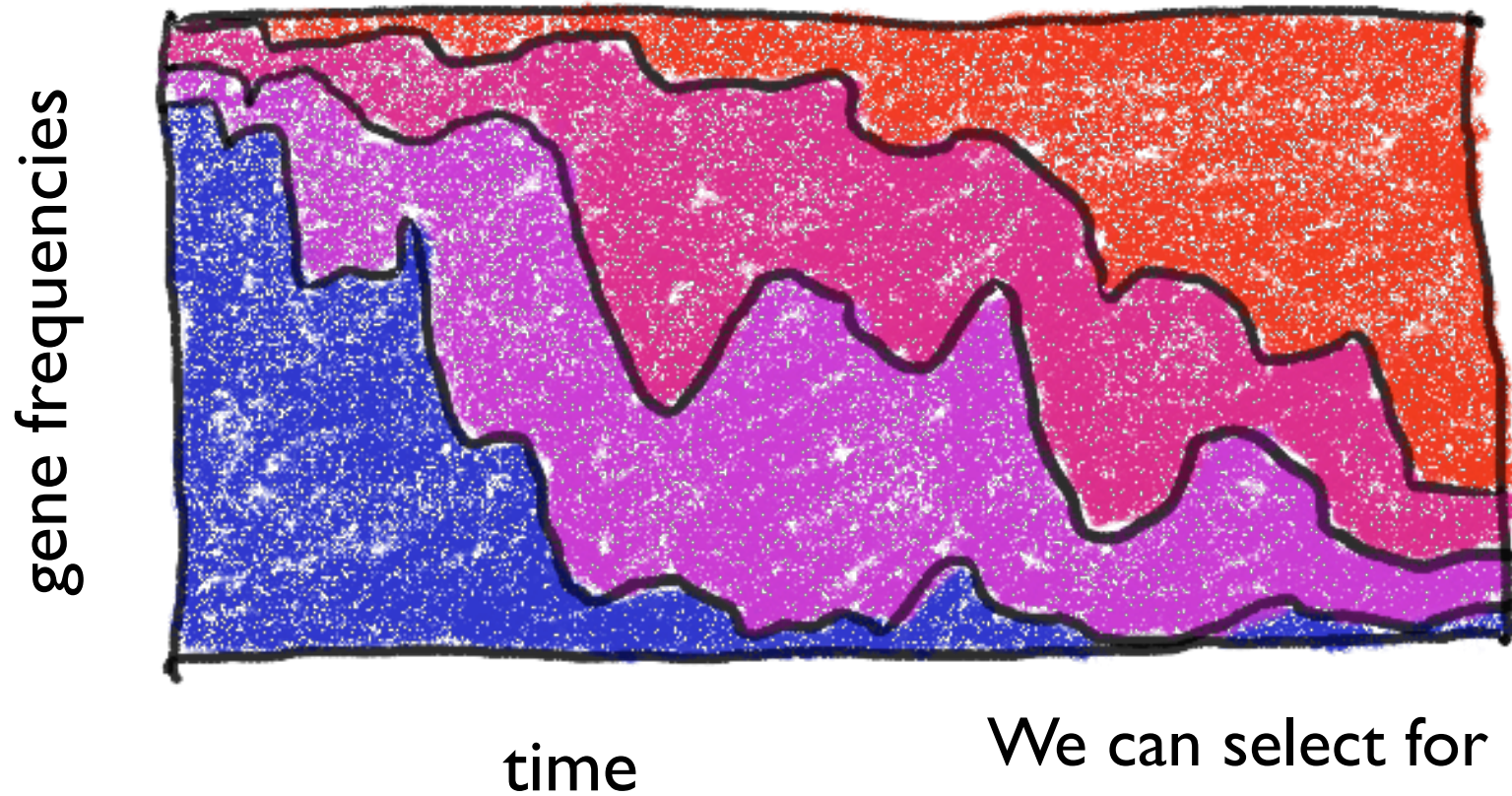


A dominates



it depends...

Gene frequencies



We can select for **redness**
but what about **greenness**???

Population Genetics

Caricature:

- 'Evolution is change in **gene frequencies**'
- 'That problem has been solved long ago'
- 'The big problem is to explain **speciation**'

Game Theory

Game Theory

First developments during 2nd World War

Then applied to Sociology

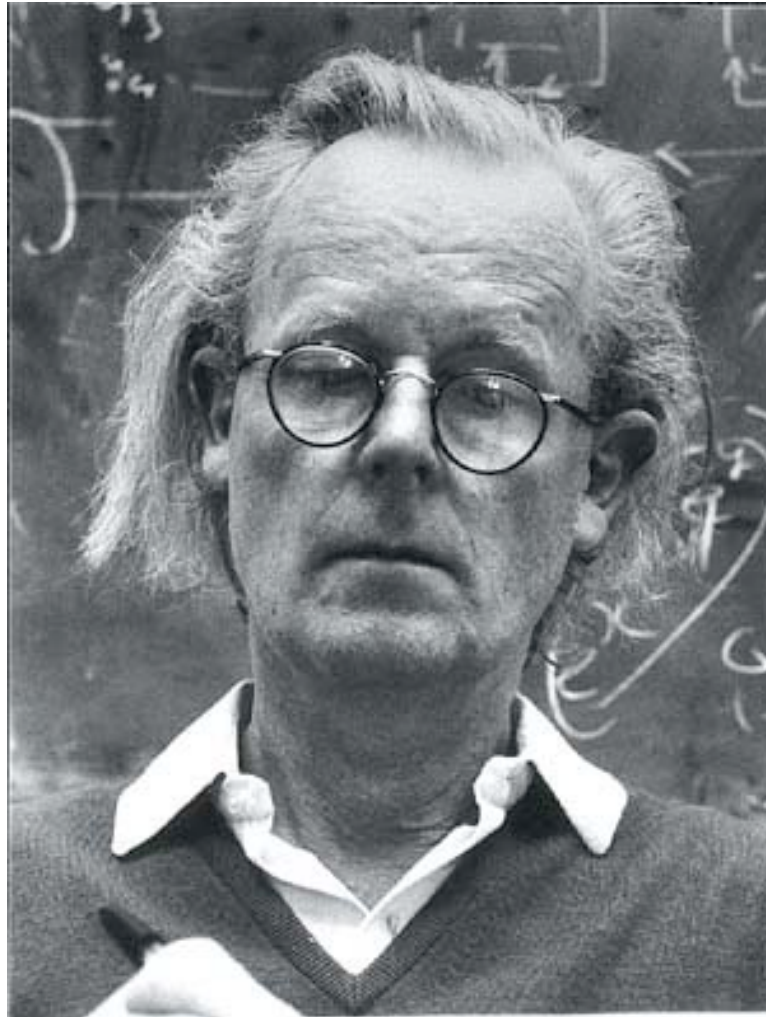
- Why do individuals **cooperate**?

Applied to Behavioural Ecology

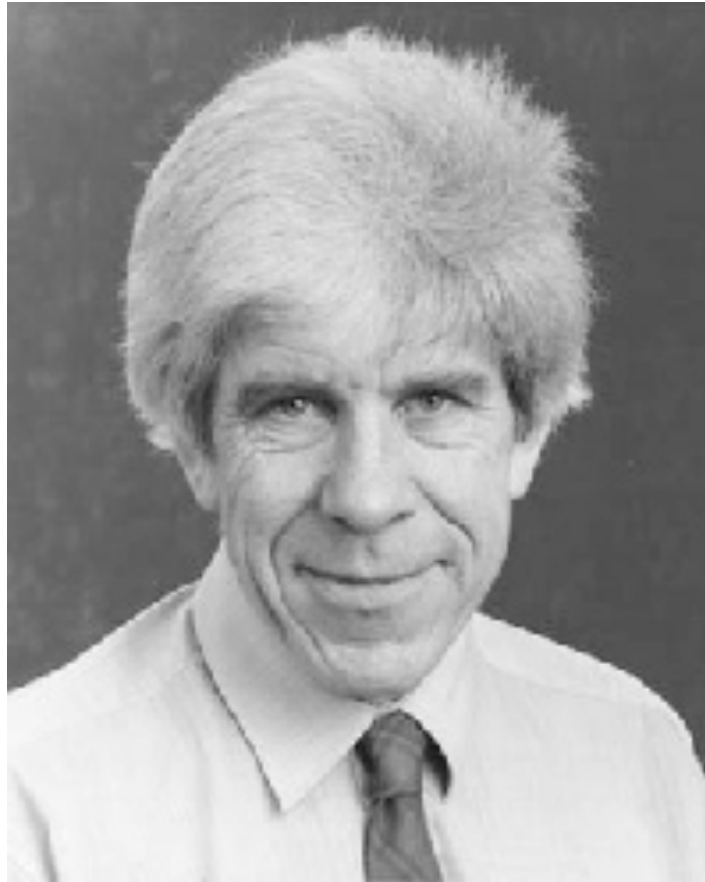
- Interactions among individuals

Bill Hamilton
John Maynard Smith

John Maynard Smith



Bill Hamilton



Evolutionary Game Theory

Observation: fighting animals rarely kill

Why such **restraint**?

Hawk-Dove Game

Maynard Smith & Price 1971

Game Theory

Individuals may choose among a range of **strategies**

Sometimes finding the **optimum strategy** is easy

Often, however, **payoffs** depend on what others do

The Hawk-Dove Game

your opponent

H

D

H

$$\frac{1}{2}(V-C)$$

V

you

D

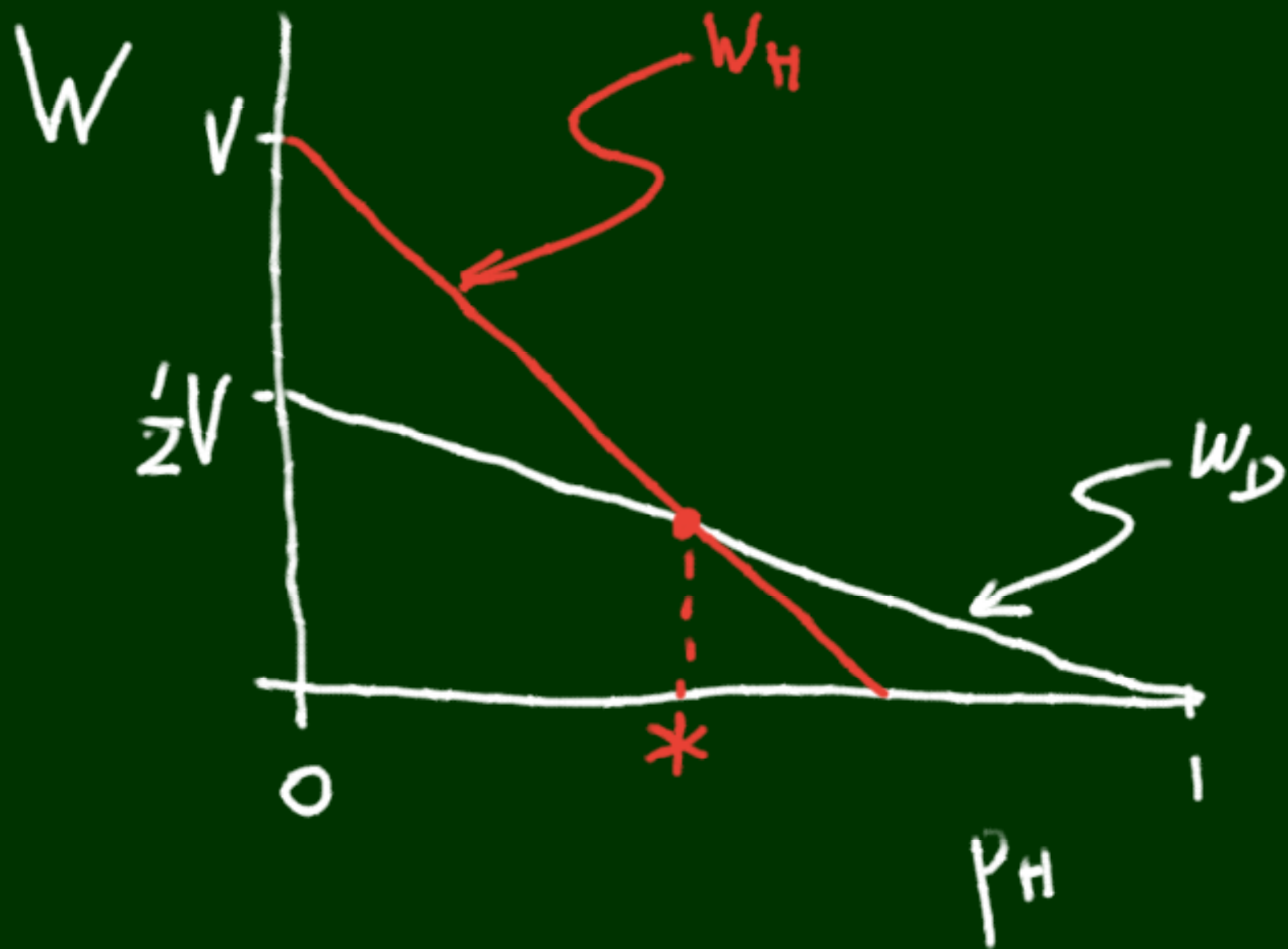
0

$$\frac{1}{2}V$$

P_H : proportion Hawks

$$\begin{aligned} W_H &= P_H \frac{1}{2}(V-C) + (1-P_H)V \\ &= V - \frac{1}{2}(V+C)P_H \end{aligned}$$

$$\begin{aligned} W_D &= P_H \cdot 0 + (1-P_H)\frac{1}{2}V \\ &= \frac{1}{2}V - \frac{1}{2}VP_H \end{aligned}$$



Evolutionarily Stable Strategies

If $p_H < p^*$ (few Hawks) then play 'Hawk'

If $p_H > p^*$ (many Hawks) then play 'Dove'

If $p_H = p^*$ both 'Hawk' and 'Dove' do equally well

A resident strategy that plays 'Hawk' with probability p^* cannot be beaten

Formalised in concept of **ESS**

John Maynard Smith,
Richard Dawkins

Evolutionary Stability

If for all strategies $J \neq I$

$$W(I|I) > W(J|I)$$

then strategy I is an **ESS**

If $W(I|I) = W(J|I)$ then I is ESS if $W(I|J) > W(J|J)$

- Maynard Smith & Price's second condition

convergence
stability

Evolutionary Game Theory

Caricature:

- 'The **fitness** of an individual depends
- on the **strategies** it adopts
- (which can be either **pure** or **mixed**)
- but also depends on the **resident** strategies
- according to the **payoff function**'

Evolutionary Game Theory

Problems

- where do the **strategies** come from?
 - Physiology?
 - Developmental genetics?
 - Behaviour?
 - Life History Theory?
- where does the **payoff function** come from?

Example: Sex Allocation

In many species, mothers can decide the sex of their offspring

- Strategy = {% sons, % daughters}

Fischer in the 30s:

- produce 50% daughters

Hamilton in the 60s:

- depends on mating structure
- biased sex ratios

Ex: Habitat Selection

In many spatially heterogeneous environments, individuals can decide

where to go

Often, payoffs depend on where others go

Q1: where should you go ?

Q2 (knowing A1) where does everybody go?

Prediction: Ideal Free Distribution

- nobody gains by moving to another place

Evolutionary Game Theory

Where does the payoff function come from?

- Fitness = Lifetime reproductive successes
- If Fitness $> 1 \Rightarrow$ Invasion
- Life History Theory



Important Insights

Population Genetics

- **mutant** genotypes may generate new phenotypes

Game Theory

- **outcome of interaction** depends on conditions

Life History Theory

- rare mutants will try to **optimize** their strategies

Ecosystem Dynamics

- **invasion** of rare species, **density dependence**

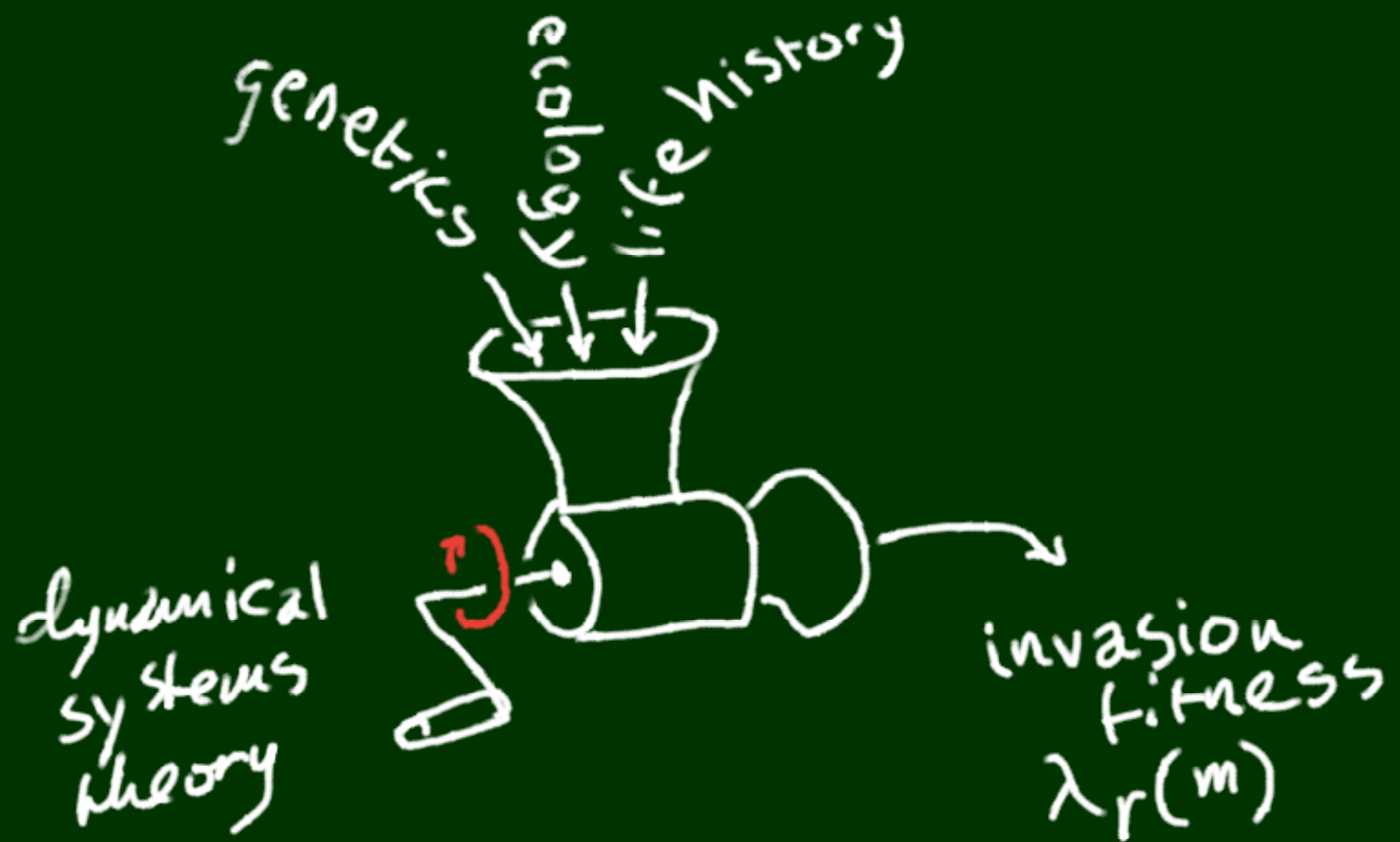
Adaptive Dynamics

Adaptive Dynamics

Caricature

- ‘New **mutants** may appear
- initially **rare**
- whose **invasion fitness**
- depends on the **resident attractor**’

Peter Hammerstein, Ilan Eshel, Hans Metz,
David Rand, Geza Meszena,
Ulf Dieckmann,
Stefan Geritz, Eva Kisdi.

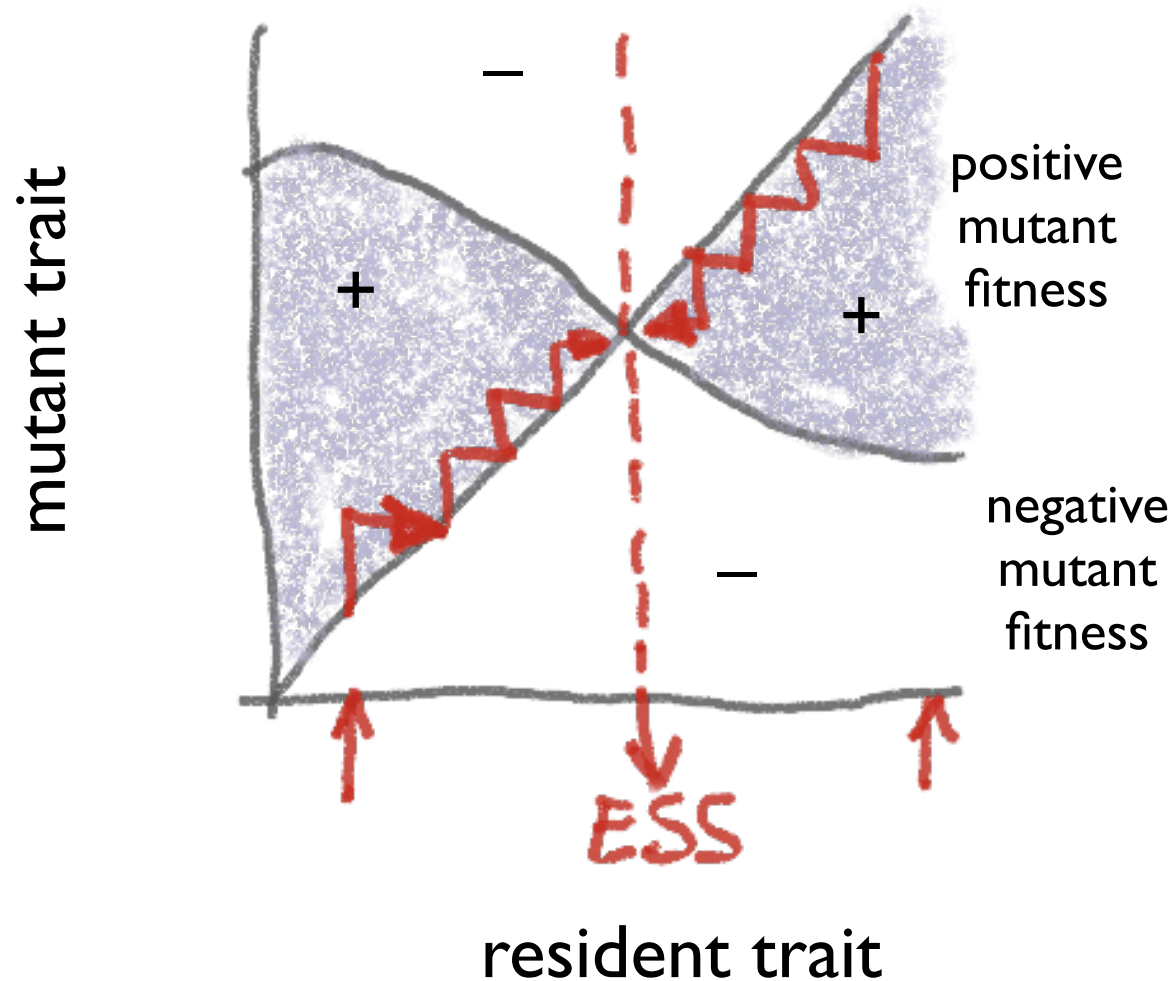


Adaptive Dynamics

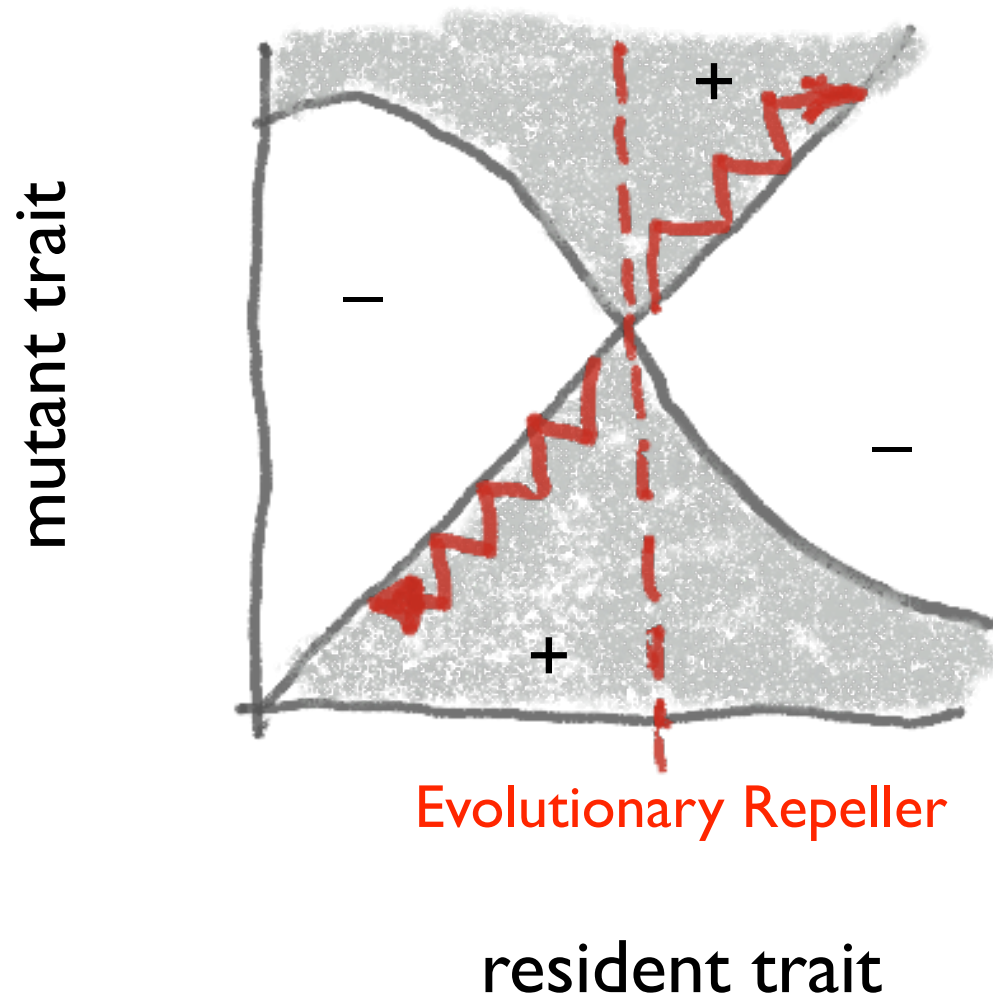
Practical Method

- monomorphic population trait a
- resident dynamics
- attractor
- mutant invasion
- pairwise invasibility plot (PIP)

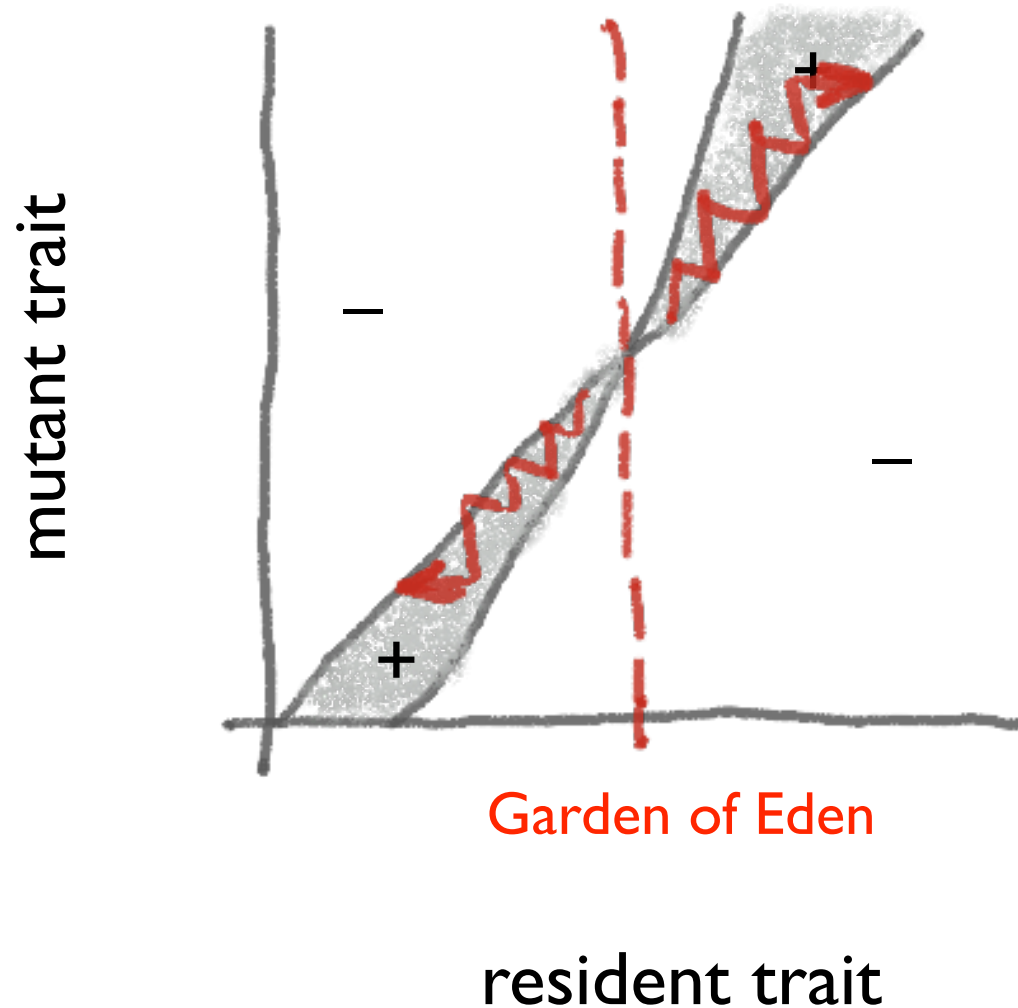
Pairwise Invasibility Plot



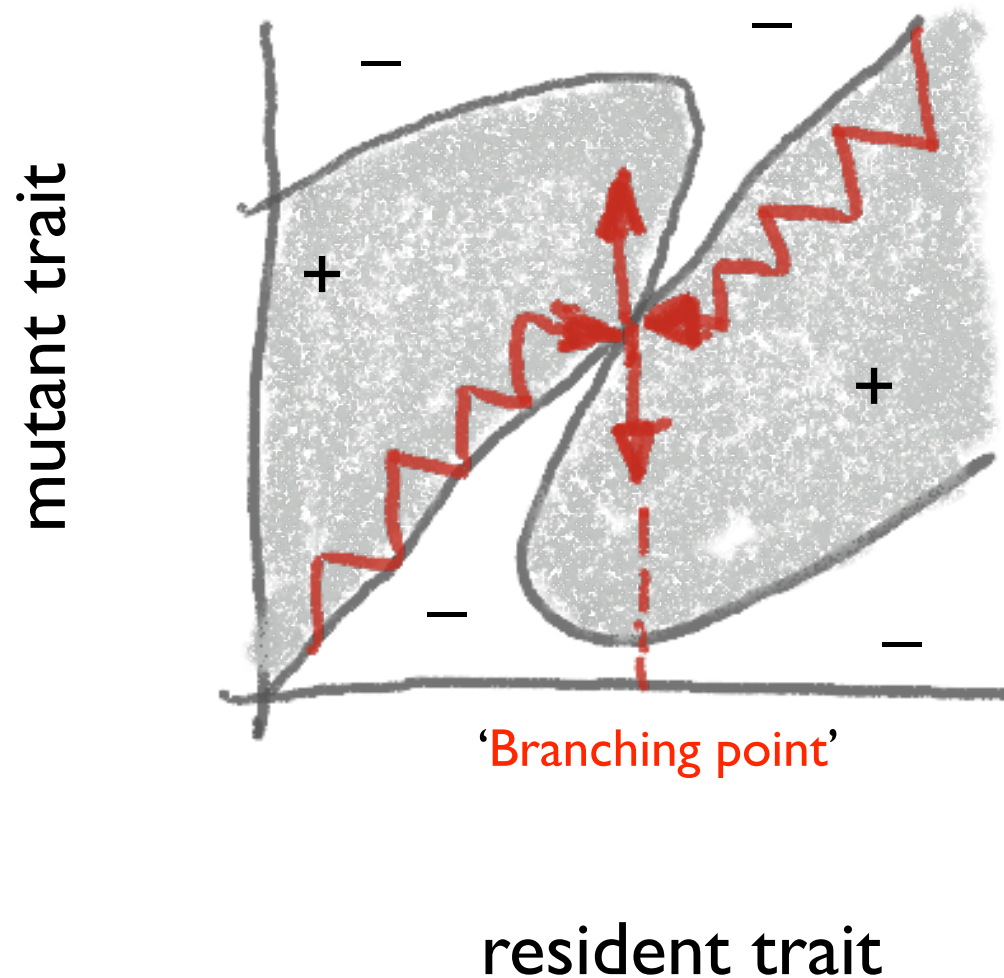
Pairwise Invasibility Plot



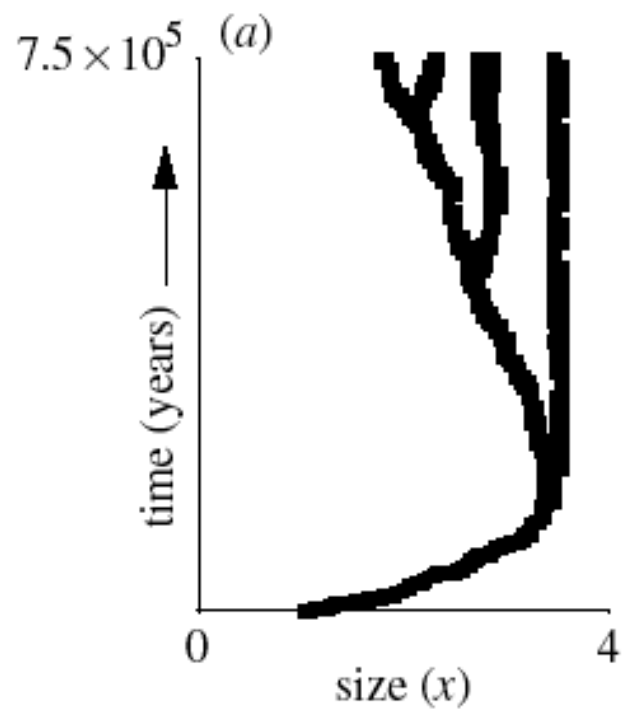
Pairwise Invasibility Plot

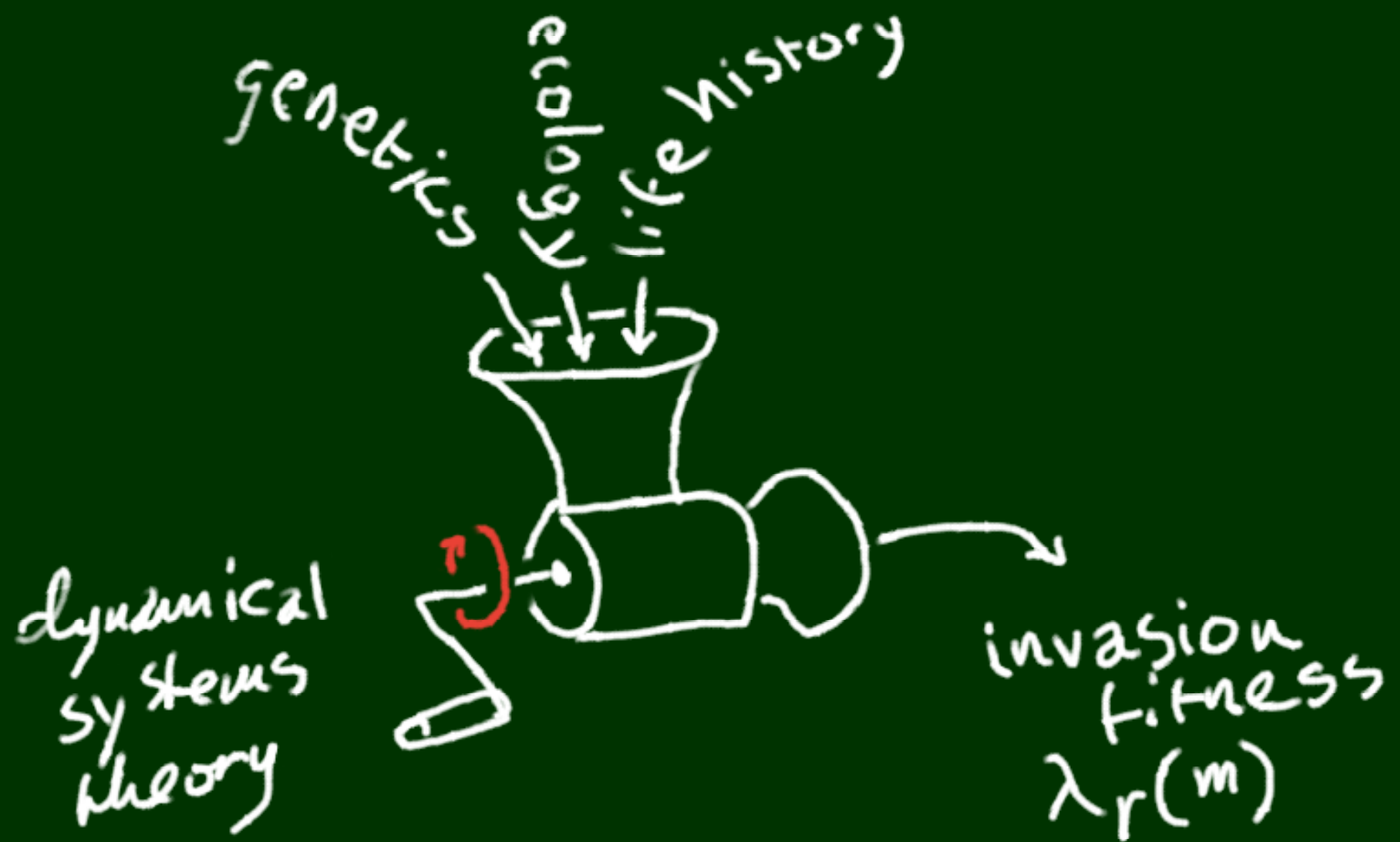


Pairwise Invasibility Plot



Kisdi & Geritz





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